



ProtoMF: Prototype-based Matrix Factorization for Effective and Explainable Recommendations



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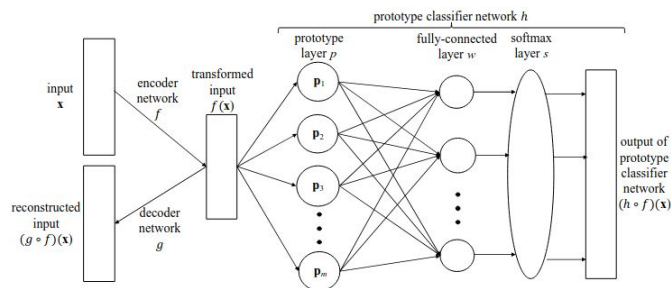


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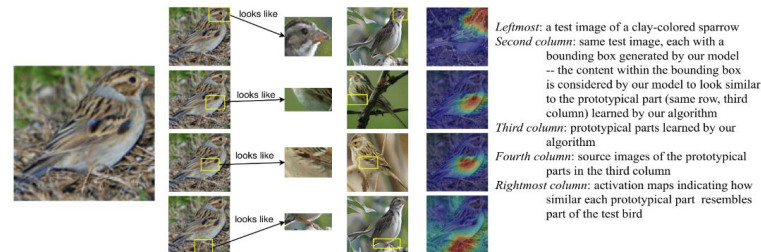


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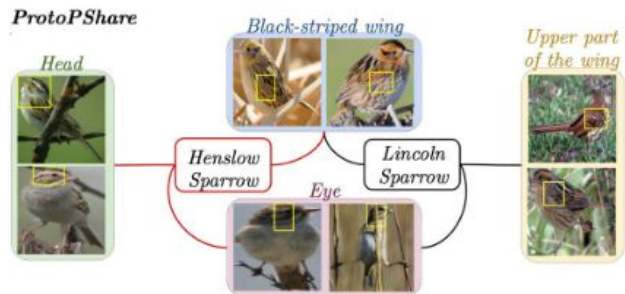
Prototype-based Machine Learning Models



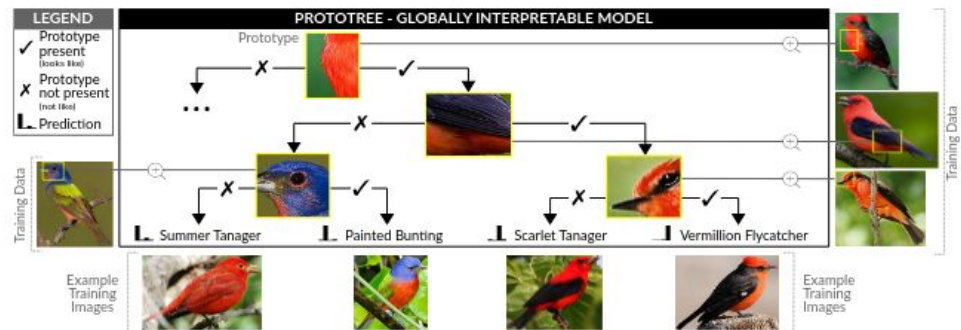
[1] Li, Oscar, et al. "Deep learning for case-based reasoning through prototypes: A neural network that explains its predictions." *AAAI* 2018.



[2] Chen, Chaofan, et al. "This looks like that: deep learning for interpretable image recognition." *NeurIPS* 2019.



[3] Rymarczyk, Dawid, et al. "Protopshare: Prototypical parts sharing for similarity discovery in interpretable image classification." *SIGKDD* 2021.



[4] Nauta, Meike, et al. "Neural prototype trees for interpretable fine-grained image recognition." *CVPR* 2021.

Prototypes

“A Prototype is an object that is representative of a set of similar instances and is part of the observed points, or it is an artifact summarizing a subset of them with similar characteristics”

[5] Guidotti, Riccardo, et al. "A survey of methods for explaining black box models." CSUR 2018.

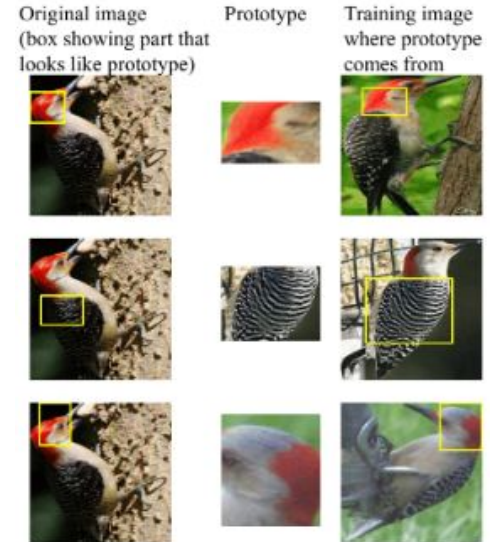


Data points



Prototypes

[1] Li, Oscar, et al. "Deep learning for case-based reasoning through prototypes: A neural network that explains its predictions." AAAI 2018.

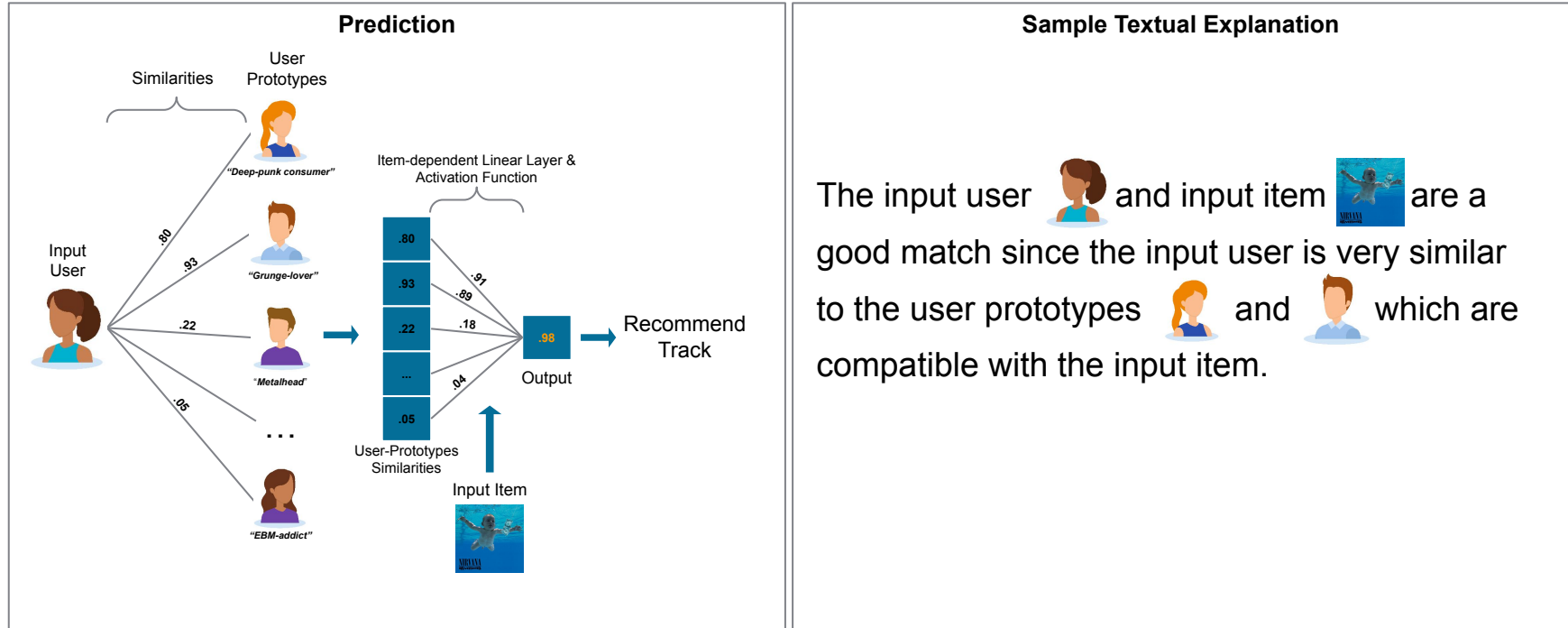


[2] Chen, Chaofan, et al. "This looks like that: deep learning for interpretable image recognition." NeurIPS 2019.

Aim:

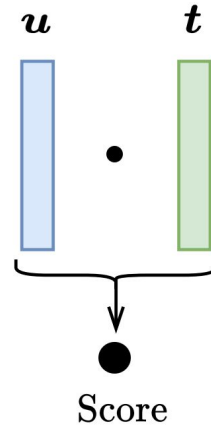
Explain recommendations of matrix factorization approaches using item and user prototypes.

Prototype-based Recommender Systems



Prototyped-based Matrix Factorization (ProtoMF)

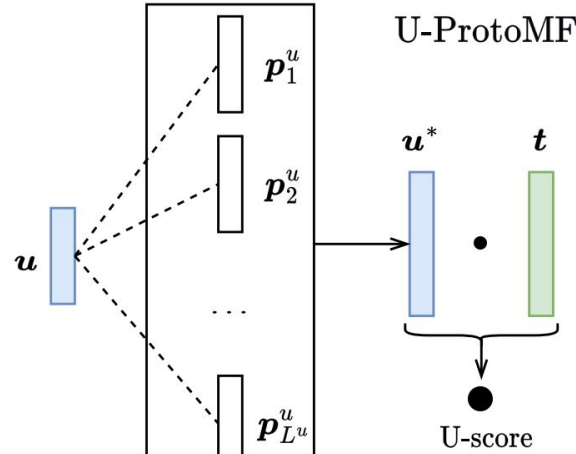
Matrix Factorization



$$\mathcal{L}_{rec}(I, \Theta) = - \sum_{(u,t) \in I} \ln p(t|u) + \lambda_{L2} \|\Theta\|, \quad p(t|u) = \frac{e^{\text{Score}(u,t)}}{\sum_{j=1}^M e^{\text{Score}(u,t_j)}}$$

- [6] Koren, Yehuda, et al.. "Matrix factorization techniques for recommender systems." Computer 2009.
[7] Rendle, Steffen, et al. "BPR: Bayesian personalized ranking from implicit feedback." UAI 2009.

User Prototype Matrix Factorization (U-ProtoMF)



$$\mathbf{u}^* = \begin{bmatrix} \text{sim}(\mathbf{u}, \mathbf{p}_1^u) \\ \dots \\ \text{sim}(\mathbf{u}, \mathbf{p}_{L^u}^u) \end{bmatrix} \in \mathbb{R}^{L^u}, \quad \text{sim}(\mathbf{a}, \mathbf{b}) = 1 + \frac{\mathbf{a}^\top \mathbf{b}}{\|\mathbf{a}\| \cdot \|\mathbf{b}\|}$$

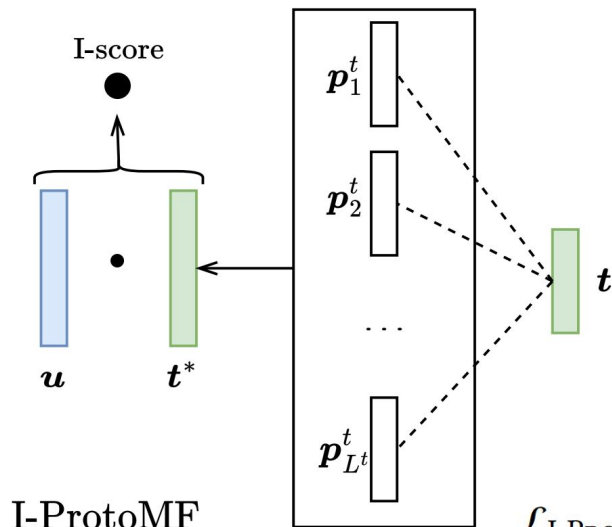
$$\text{U-score}(\mathbf{u}, \mathbf{t}) = \sum_{l=1}^{L^u} s_l^{\text{user}}, \quad \mathbf{s}^{\text{user}} = \mathbf{u}^* \odot \mathbf{t}$$

$$\mathcal{L}_{\text{U-PROTO}} = \mathcal{L}_{\text{rec}} + \lambda_1 R_{\{\mathcal{P}^u \rightarrow \mathcal{U}\}} + \lambda_2 R_{\{\mathcal{U} \rightarrow \mathcal{P}^u\}}$$

$$R_{\{\mathcal{U} \rightarrow \mathcal{P}^u\}} = -\frac{1}{N} \sum_{i=1}^N \max_{l \in [1, \dots, L^u]} \text{sim}(\mathbf{u}_i, \mathbf{p}_l^u)$$

$$R_{\{\mathcal{P}^u \rightarrow \mathcal{U}\}} = -\frac{1}{L^u} \sum_{l=1}^{L^u} \max_{i \in [1, \dots, N]} \text{sim}(\mathbf{u}_i, \mathbf{p}_l^u)$$

Item Prototype Matrix Factorization (I-ProtoMF)



$$t^* = \begin{bmatrix} \text{sim}(t, p_1^t) \\ \dots \\ \text{sim}(t, p_{L^t}^t) \end{bmatrix} \in \mathbb{R}^{L^t}$$

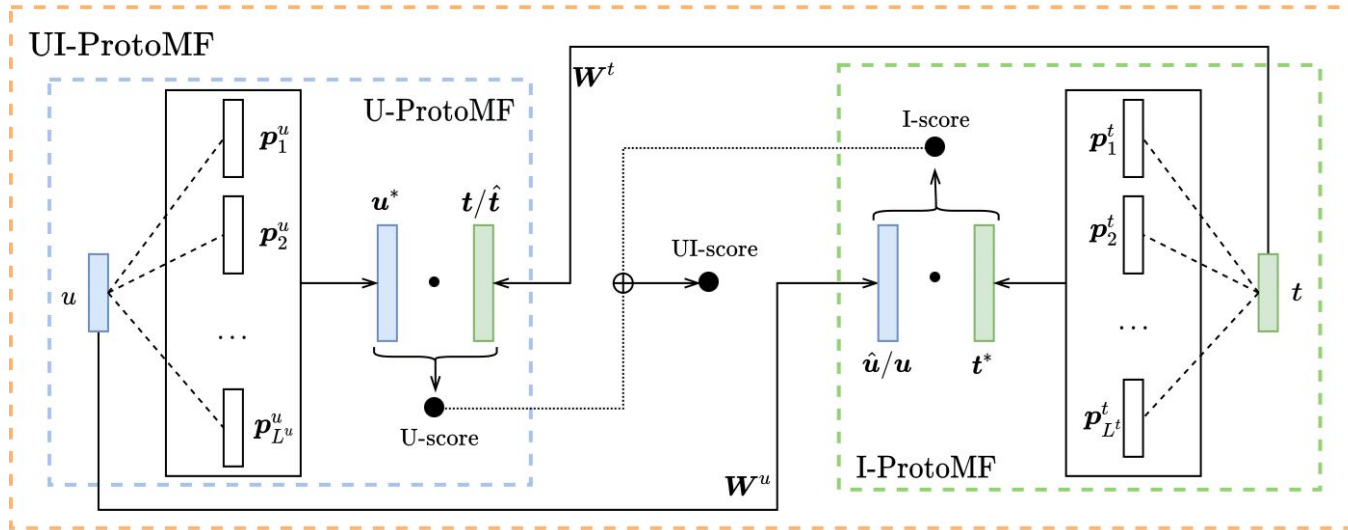
$$\text{I-score}(u, t) = \sum_{l=1}^{L^t} s_l^{\text{item}}, \quad s^{\text{item}} = t^* \odot u$$

$$\mathcal{L}_{\text{I-PROTO}} = \mathcal{L}_{\text{rec}} + \lambda_3 R_{\{\mathcal{P}^t \rightarrow \mathcal{T}\}} + \lambda_4 R_{\{\mathcal{T} \rightarrow \mathcal{P}^t\}}$$

$$R_{\{\mathcal{P}^t \rightarrow \mathcal{T}\}} = -\frac{1}{L^t} \sum_{l=1}^{L^t} \max_{j \in [1, \dots, M]} \text{sim}(t_j, p_l^t)$$

$$R_{\{\mathcal{T} \rightarrow \mathcal{P}^t\}} = -\frac{1}{M} \sum_{i=1}^M \max_{l \in [1, \dots, L^t]} \text{sim}(t_i, p_l^t)$$

User-Item Prototype Matrix Factorization (UI-ProtoMF)



$$\text{UI-score}(u, t) = \text{U-score}(u, t) + \text{I-score}(u, t)$$

$$\hat{u} = W^u u \in \mathbb{R}^{L^t}, \quad \hat{t} = W^t t \in \mathbb{R}^{L^u}$$

$$\mathcal{L}_{\text{UI-PROTO}} = \mathcal{L}_{\text{U-PROTO}} + \mathcal{L}_{\text{I-PROTO}}$$

Experiment Setup

- Datasets:
 - *MovieLens-1M* [8]
 - *LFM2B-1Month* [9]
 - *Amazon Video Games* [10]
- Baselines:
 - *Matrix Factorization* [6]
 - *Representative-based Matrix Factorization* [11]
 - *Anchor-based Collaborative Filtering* [12]
- *NDCG* and *Hit Ratio* at 5, 10, 50.
- Statistical tests assessing the improvements.
- Extensive hyperparameter optimization.

	ML-1M	LFM2B-1MON	AMAZONVID
# Users	6,034	3,555	6,950
# Males/Females	4,326/1,708 (72%/28%)	2,965/590 (83%/17%)	-
# Items	3,125	77,985	14,494
# Interactions	574,376	877,365	132,209

Table 1: Statistics of the datasets after filtering.

[8] Harper, F. Maxwell, and Joseph A. Konstan. "The Movielens Datasets: History and Context." TIS 2015.

[9] Schedl, Markus, et al. "LFM-2b: A Dataset of Enriched Music Listening Events for Recommender Systems Research and Fairness Analysis." CHIIR 2022.

[10] McAuley, Julian, et al. "Image-based Recommendations on Styles and Substitutes." SIGIR 2015.

[6] Koren, Yehuda, et al.. "Matrix factorization techniques for recommender systems." Computer 2009.

[11] Liu, Nathan N., et al. "Wisdom of the better few: cold start recommendation via representative based rating elicitation." RecSys 2011.

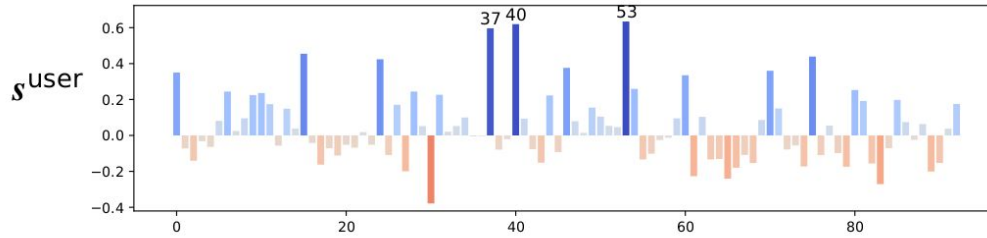
[12] Barkan, Oren, et al. "Anchor-based collaborative filtering." CIKM 2021.

Evaluation Results (@10)

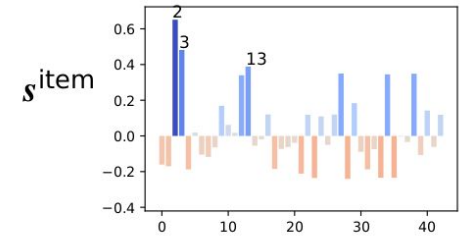
Model	ML-1M		AMAZONVID		LFM2B-1MON	
	NDCG	HITRATIO	NDCG	HITRATIO	NDCG	HITRATIO
MF	.326	.571	.140	.255	.118	.215
RBMF	.282	.505	.093	.166	.279†	.384†
ACF	.335	.597†	.202†	.392†	.291†	.517†
U-PROTOMF	.333	.583	.152†	.276†	.179†	.322†
I-PROTOMF	.303	.544	.194†	.371†	.251†	.457†
UI-PROTOMF	.383†‡	.657†‡	.220†‡	.401†	.347†‡	.579†‡

Table 2: Evaluation results w.r.t. accuracy metrics at cutoff 10. The sign † indicates significant improvement over MF while ‡ indicates significant improvement over ACF.

Explaining UI-ProtoMF Recommendations



(a) U-ProtoMF



(b) I-ProtoMF

User Prototype 53	User Prototype 40	User Prototype 37	Item Prototype 3	Item Prototype 2	Item Prototype 13
Roman Holiday <i>Comedy Romance</i>	Runaway Bride <i>Comedy Romance</i>	Cinderella <i>Anim. Children's Musical</i>	City of Angels <i>Romance</i>	Broadway Melody, The <i>Musical</i>	Chambermaid on the Titanic, The <i>Romance</i>
To Catch a Thief <i>Com. Romance Thriller</i>	She's All That <i>Comedy Romance</i>	Little Mermaid, The <i>Anim. Child. Com. Musical</i>	It Could Happen to You <i>Drama Romance</i>	Slipper and the Rose, The <i>Adventure Musical Romance</i>	Dreaming of Joseph Lees <i>Romance</i>
Sabrina <i>Comedy Romance</i>	Affair to Remember, An <i>Romance</i>	Sleeping Beauty <i>Anim. Children's Musical</i>	Walk in the Clouds, A <i>Drama Romance</i>	Penny Serenade <i>Drama Romance</i>	Passion of Mind <i>Romance Thriller</i>
Sleepless in Seattle <i>Comedy Romance</i>	Double Jeopardy <i>Action Thriller</i>	She's All That <i>Comedy Romance</i>	One Fine Day <i>Drama Romance</i>	Perils of Pauline, The <i>Comedy</i>	Golden Bowl, The <i>Drama</i>
While You Were Sleeping <i>Comedy Romance</i>	Ever After: A Cinderella Story <i>Drama Romance</i>	101 Dalmatians <i>Animation Children's</i>	Sommersby <i>Drama Mystery Romance</i>	Damsel in Distress, A <i>Comedy Musical Romance</i>	Up at the Villa <i>Drama</i>

Thank you for your attention!

Code, dataset splits, and more are hosted on
<https://github.com/hcai-mms/ProtoMF>



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